Appendix C

Temperature Scales and Telescope Efficiencies

The calibration mode used for essentially all spectral line observations at the 12m is the chopper wheel method (see Ulich & Haas, 1976, ApJS, 30, 247 for a detailed description of this technique). The chopper wheel technique corrects for atmospheric attenuation and several telescope losses. In the following, I describe the temperature scale used at the 12m and how it relates to temperature scales used at other millimeter wavelength observatories.

C.1 Definitions

In the following I define the terms used in the subsequent temperature scale and telescope efficiency discussion. I have tried to adopt a similar nomenclature to that used in Kutner & Ulich (1981, ApJ, 250, 341). Note that throughout this discussion when I refer to a "temperature" I am actually referring to the effective source radiation temperature J(v,T), which is defined as:

$$J(v,T) \equiv \left(\frac{hv}{k}\right) \left(\frac{1}{\exp\left(\frac{hv}{kT}\right)-1}\right)$$
 (C.1)

General Terms

 $\Omega_s \equiv \text{Solid}$ angle subtended by the source

 $\Omega_d \equiv \text{Solid}$ angle subtended by the central diffraction beam pattern of the telescope

 $\Omega \equiv \text{Solid}$ angle on the sky

 $\Psi \equiv \text{Direction angle on the sky}$

 $P_n \equiv Normalized antenna power pattern$

 $P_{ng} \equiv Normalized Gaussian antenna power pattern$

B = Normalized source brightness distribution

 $A \equiv Air$ mass toward which the measurement is made

 $\tau_0 \equiv \text{Atmospheric optical depth at the zenith}$

 $G \equiv Maximum antenna gain$

Efficiencies

$$\eta_{\rm r} \equiv \text{Radiative efficiency}$$

$$\equiv \frac{G}{4\pi} \iint_{4\pi} \mathbf{P}_{n}(\Omega) d\Omega \qquad (C.2)$$

$$\eta_{\text{rss}} \equiv \text{Rearward Scattering and spillover efficiency}$$

$$\equiv \frac{\iint_{2\pi} P_n(\Omega) d\Omega}{\iint_{4\pi} P_n(\Omega) d\Omega} \tag{C.3}$$

$$\eta_{l} \equiv \eta_{r} \eta_{rss}$$
(C.4)

$$\eta_{\text{fss}} \equiv \text{Forward scattering and spillover efficiency}$$

$$\equiv \frac{\iint_{\Omega_d} P_n(\Omega) d\Omega}{\iint_{2\pi} P_n(\Omega) d\Omega} \tag{C.5}$$

$$\eta_{\text{mb}} \equiv \text{Main beam efficiency}$$

$$\equiv \frac{\iint_{4\pi} P_{ng}(\Omega) d\Omega}{\iint_{4\pi} P_{n}(\Omega) d\Omega} \tag{C.6}$$

$$\eta_{\rm cmb}$$
 \equiv Efficiency at which the source couples to the main diffraction beam of the telescope
$$\equiv \frac{\iint_{\Omega_s} P_n(\Psi - \Omega) B_n(\Psi) d\Psi}{\iint_{4\pi} P_{ng}(\Omega) d\Omega} \tag{C.7}$$

$$\eta_{c} \equiv \text{Efficiency at which the source couples to the telescope beam} \\
\equiv \eta_{cmb}\eta_{mb} \qquad (C.8) \\
\equiv \frac{\iint_{\Omega_{s}} P_{n}(\Psi - \Omega)B_{n}(\Psi)d\Psi}{\iint_{\Gamma} P_{n}(\Omega)d\Omega}$$

Temperatures

 $TR \equiv Source radiation temperature$

 $TA \equiv Observed$ source antenna temperature

$$\equiv \frac{GT_R}{4\pi} \exp(-A\tau_0) \iint_{\Omega_s} P_n(\Psi - \Omega) B_n(\Psi) d\Psi \tag{C.10}$$

 $T'_A \equiv \text{Observed source}$ antenna temperature corrected for atmospheric attenuation

$$\equiv T_A \exp(A\tau_0) \tag{C.11}$$

 $T_A^* \equiv \text{Observed source}$ antenna temperature corrected for atmospheric attenuation, radiative loss and rearward scattering and spillover

$$\equiv \frac{T_A'}{\eta_r \eta_{rss}} \tag{C.12}$$

 $T_R^* \equiv \text{Observed source}$ antenna temperature corrected for atmospheric attenuation, radiative loss and rearward and forward scattering and spillover¹

$$\equiv \frac{T_A^*}{\eta_{fss}} \tag{C.13}$$

 $\Delta T_R \equiv \text{Source radiation temperature excluding any background emission (like the cosmic$ microwave background emission)

$$\equiv T_R - T_{bg}$$

$$\equiv \frac{T_R^*}{\eta_c} \tag{C.14}$$

 $T_{mb} \equiv \text{Source brightness temperature as measured by the main diffraction beam of the}$ telescope

$$\equiv \eta_{cmb} \Delta T_R \tag{C.15}$$

C.2 Relations Between Temperature Scales

We can now combine the definitions above to derive the relations between the physical measurements and the temperature scale used at the 12m and the scales used at other telescopes. Combining the equations above, we can relate the source temperature corrected for atmospheric attenuation (T0 A) to many of the antenna and source temperatures:

$$T'_{A} = \eta_{r} \eta_{rss} \eta_{fss} \eta_{c} \Delta T_{R}$$
 (C.16)

$$= \eta_l \eta_{fss} T_R^*$$

$$= \eta_l T_A^*$$
(C.17)
(C.18)

$$= \eta_I T_A^* \tag{C.18}$$

$$= \eta_{mb} T_{mb} \tag{C.19}$$

 ${}^{1}T_{R}^{*}$ can also be defined as the source brightness temperature corrected for atmospheric attenuation, radiative loss, and rearward and forward scattering and spillover if the source is equal to or larger than the main diffraction beam.

C.3 Telescope Efficiency Measurements

Telescope efficiencies are normally calculated using a measurement of the continuum brightness of a planet (for η_{mb}) or the Moon (for η_{fss}). In the following I give the relations used to calculate several telescope efficiencies. Since the source coupling between a disk source like the planets and a Gaussian telescope beam is given by:

$$\eta_{cmb} = 1 - \exp \left[-\ln(2) \left(\frac{\theta_s}{\theta_B} \right)^2 \right]$$
(C.20)

I will use this term in the efficiency equation derivations given below.

C.3.1 Corrected Main Beam Efficiency

The efficiency factor which converts the 12m T_R^* scale to the T_{mb} scale is given by:

$$\eta_m^* = \frac{\eta_{mb}}{\eta l \eta_{fss}}$$

$$= \frac{T_R^*}{T_{mb}}$$

$$= \frac{T_R^*}{\left(T_R - T_{bg}\right) \left\{1 - \exp\left[-\ln(2)\left(\frac{\theta_s}{\theta_B}\right)^2\right]\right\}}$$
(C.21)

One can also calculate η_m^* using the Ruze equation:

$$\eta_m^* = \left[1 + \frac{A_e \theta_e^2}{A_m \theta_m^2} \right]^{-1} \tag{C.22}$$

given that:

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$$\theta_e = 2\sqrt{\ln(2)} \frac{\lambda}{\pi c_\sigma} \tag{C.23}$$

$$\theta_m = 1.22 \frac{\lambda}{D} \tag{C.24}$$

$$\frac{A_e}{A_m} = \frac{1}{\eta_{a0}} \left[\frac{2c_\sigma}{D} \right]^2 \left\{ \exp(\delta^2) - 1 \right\}$$
 (C.25)

where λ is the wavelength of observation, c_{σ} is the correlation scale size of the surface deviations (280 mm), η_{a0} is the zero wavelength aperture efficiency (0.55), and δ is the surface accuracy (75 μ m). Figure C.1 shows this relation with the actual measurements given in Table C.1.

C.3.2 Main Beam Efficiency

The efficiency factor which converts any source antenna measurement to the T_{mb} scale is given by:

$$\eta_{mb} = \frac{T_A'}{T_{mb}}$$

$$= \frac{\eta l \eta_{fss} T_R^*}{\left(T_R - T_{bg}\right) \left\{1 - \exp\left[-\ln\left(2\left(\frac{\theta_s}{\theta_B}\right)^2\right]\right\}} \tag{C.26}$$

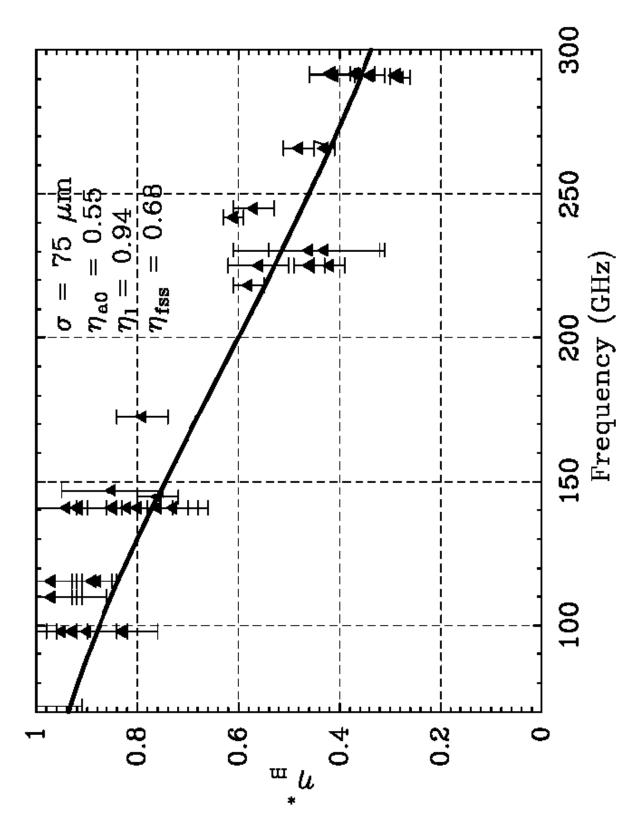


Figure C.1: Measured and theoretical estimates of η_m^* as a function of frequency.

Table C.1 lists the most recent measurements of η_m^* and η_{mb} for the planets and frequencies given.

Table C.1: 12m Telescope Efficiencies

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Frequency	Source	Source Size			η_m			η_{mb}			Date
(GHz)			rcsec	/							Measured
72.0	Jupiter	37.4	X	35.0	1.04	土	0.13	0.66	土	0.08	April 1997
98.0	Venus	12.2	X	12.2	0.90	±	0.06	0.57	±	0.04	Nov 1996
98.0	Mars	8.5	X	8.4	0.83	±	0.07	0.53	±	0.04	Jun 1997
98.0	Saturn	16.9	X	15.3	0.93	±	0.11	0.59	±	0.07	Jun 1997
109.8	Venus	22.1	X	22.1	0.97	±	0.04	0.62	±	0.02	Aug 1996
109.8	Jupiter	43.4	X	40.6	0.97	±	0.05	0.62	±	0.03	Aug 1996
109.8	Saturn	19.2	X	17.3	0.97	±	0.06	0.62	±	0.04	Aug 1996
115.3	Jupiter	43.4	X	40.6	0.88	±	0.04	0.56	±	0.02	Aug 1996
115.3	Saturn	19.2	X	17.3	0.97	±	0.06	0.62	±	0.04	Aug 1996
140.8	Venus	13.4	X	13.4	0.73	±	0.05	0.47	±	0.03	Nov 1996
140.8	Mars	5.5	X	5.5	0.85	±	0.07	0.54	±	0.04	Nov 1996
140.8	Jupiter	35.5	X	33.2	0.82	±	0.09	0.52	±	0.06	Nov 1996
140.8	Saturn	19.1	X	17.2	0.92	±	0.09	0.59	±	0.06	Nov 1996
140.8	Uranus	3.5	X	3.5	0.80	±	0.10	0.51	±	0.06	Nov 1996
140.8	Neptune	2.2	X	2.2	0.76	±	0.10	0.48	±	0.06	Nov 1996
144.6	Saturn	17.4	X	15.7	0.76	±	0.04	0.48	±	0.03	Jun 1996
218.2	Saturn	18.0	X	16.1	0.58	±	0.03	0.37	±	0.02	Nov 1995
230.5	Saturn	19.5	X	17.6	0.43	±	0.11	0.27	±	0.07	Oct 1996
230.5	Uranus	3.6	X	3.5	0.46	±	0.15	0.29	±	0.09	Oct 1996
244.9	Mars	7.5	X	7.5	0.57	±	0.04	0.36	±	0.02	Dec 1996
265.9	Mars	5.5	X	5.5	0.48	±	0.03	0.31	±	0.02	Nov 1996
291.8	Mars	7.1	X	7.1	0.42	±	0.04	0.27	±	0.02	Dec 1996
291.8	Saturn	17.8	X	16.1	0.37	±	0.04	0.24	±	0.02	Dec 1996